

P. Vietnam Training

Time limit: 1 second
Memory limit: 256 MBytes

Description

This is an interactive problem. It's 1971 and the Vietnam War is raging. Nguyen Phan is a vietnamese general and he wants to test a new strategy. His task is to make reconnaissance more efficient on the battlefield, using soldiers and tunnels. There are n soldiers placed at integer coordinates on the battlefield. The soldiers are indexed with integers from 1 to n . The i -th soldier has coordinates (x_i, y_i) , which are secret. Two soldiers are visible to each other if there are no other soldiers on the straight segment between them.

With a single command (query), Nguyen Phan can order one of his soldiers to travel through the underground tunnels and pop his head out at coordinates x and y . He can get the following response:

- if at (x, y) there is another soldier with index i , then the soldier that was sent through the tunnels will go back to the base and tell Nguyen Phan the index of the soldier that was already there, $-i$;
- otherwise, the soldier that was sent through the tunnels will STAY at coordinates (x, y) with index t , where t is the total current number of soldiers on the battlefield, including the one sent with this command; the soldier sent returns the list of the indices of all soldiers visible from (x, y) .

Nguyen Phans task is to find the coordinates of the initial n soldiers using a limited number of commands! Because you are his assistant, he wants YOU to carry out this task.

Interaction Protocol

The first line contains a single integer n ($1 \leq n \leq 400$), the number of soldiers. The secret coordinates satisfy $0 \leq x_i, y_i \leq 100$ and all n locations are distinct.

To ask a query, output `?` followed by two integers x and y ($-10^9 \leq x, y \leq 10^9$). If there is already a soldier in (x, y) , the result will be $-i$, where i is the index of that soldier. Otherwise the result is given by an integer k , the number of soldiers visible from (x, y) , followed by k integers i_1, \dots, i_k , the indices of the visible soldiers in increasing order ($i_j < i_{j+1}$ for all $1 \leq j < k$). You can use at most 400 queries.

Once you have determined the coordinates of the original soldiers, first output `!` in a single line. Then output n lines, with two integers x, y_i in the i -th line, being the coordinates of the i -th soldier. After that your program should terminate.

Example

Standard input	Standard output
3	? 2 3
2 1 3	? 6 6
3 1 2 4	? 6 6
-5	? 1 11
4 2 3 4 5	? 4 7
-2	!
	3 5
	4 7
	2 8